

# Team Road Runner



Team 3: Arnav Dhamija, Luca Scheuer, Saumya Shah  
Instructor: Rahul Mangharam(rahulm@seas)  
ESE615 Autonomous Racing

# Content

---

## I. Milestone II approach

- Pure pursuit
- CMAES
- Splines

## II. Milestone III approach

- RRT + Pure Pursuit
- Advancements

## III. Milestone IV approach

- MPC
- Lane switching

## IV. Miscellaneous



# Milestone 2 approach

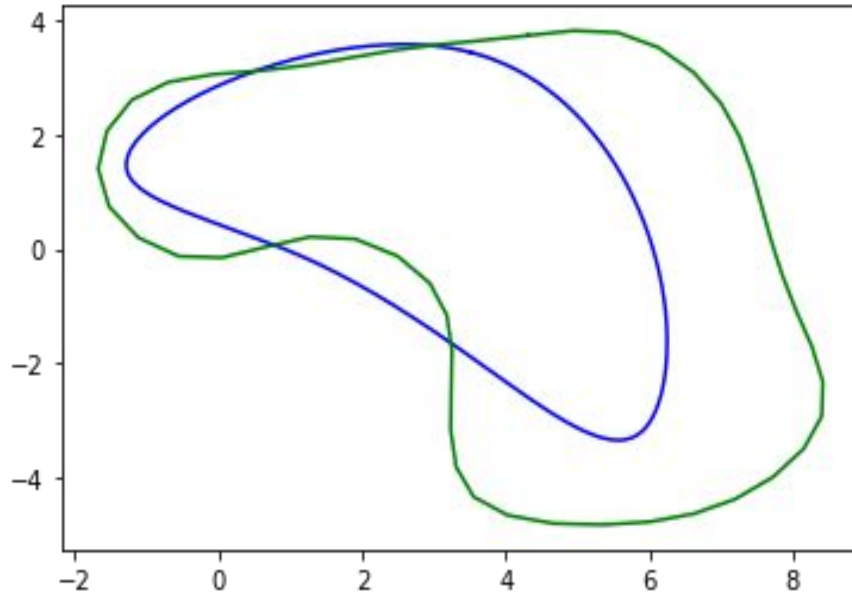
---

# Optimal Trajectory

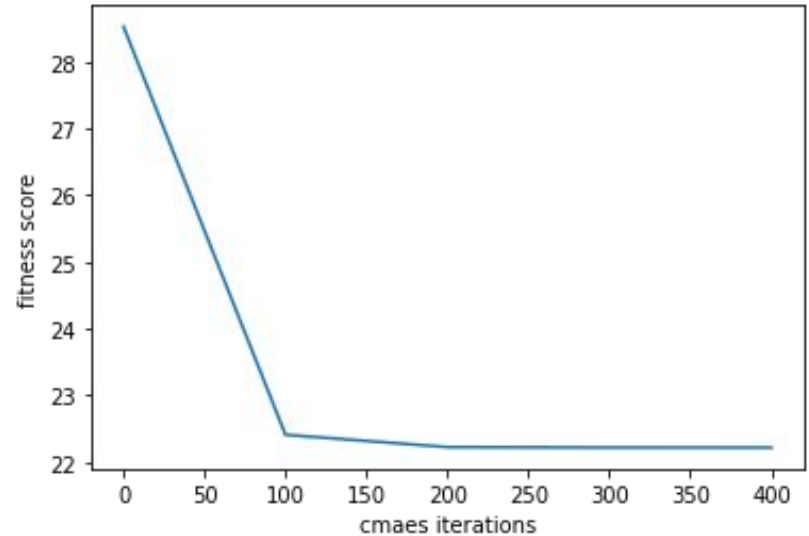
- CMAES for trajectory generation
  - Sparsely sampled centerline points for CMAES initialization
  - Polar constraints for CMA-ES solver
    - Solves for  $R_i, \theta_i$
    - No box transformations involved
    - Simplified constraints to bounds as required
  - Regularized spline fit on the sampled points
  - Fitness calculated as time to complete the loop with curvature dependent velocity profile (leads to approx. minimum curvature trajectory)
  - Regularized spline on final solution sampled for 500 points

# Optimal Trajectory

CMAES trajectory vs Centerline



Fitness curve vs optimization iters



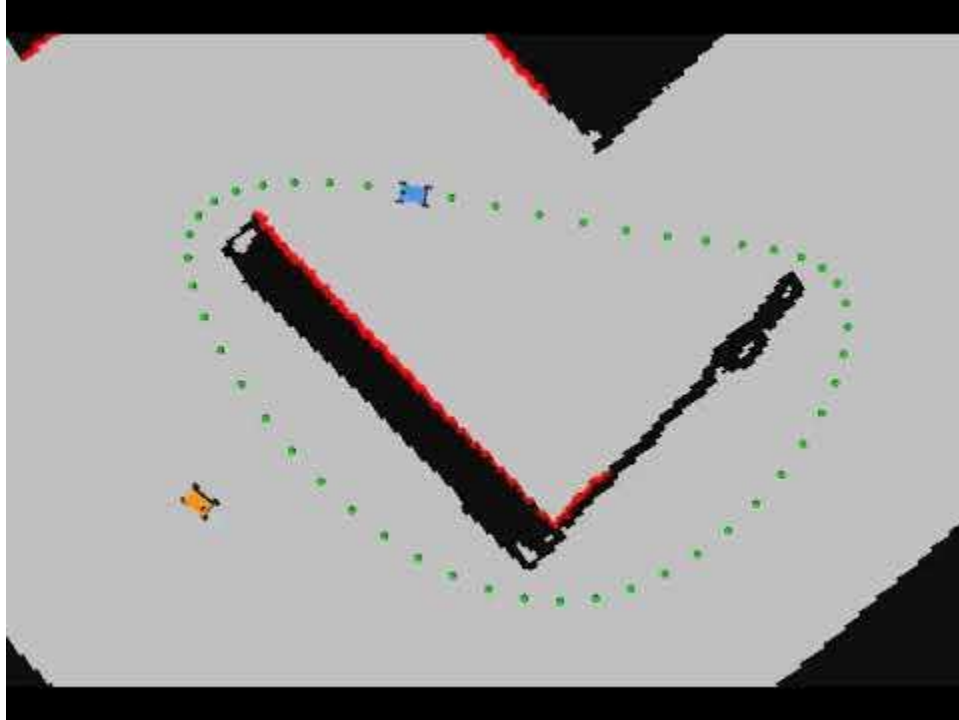
# Optimal Trajectory

---

- Pure Pursuit

- Used Pure Pursuit with lookahead to follow the way points at full speed
- Cons: No drift control

# Milestone 2





# Milestone 3 approach

---

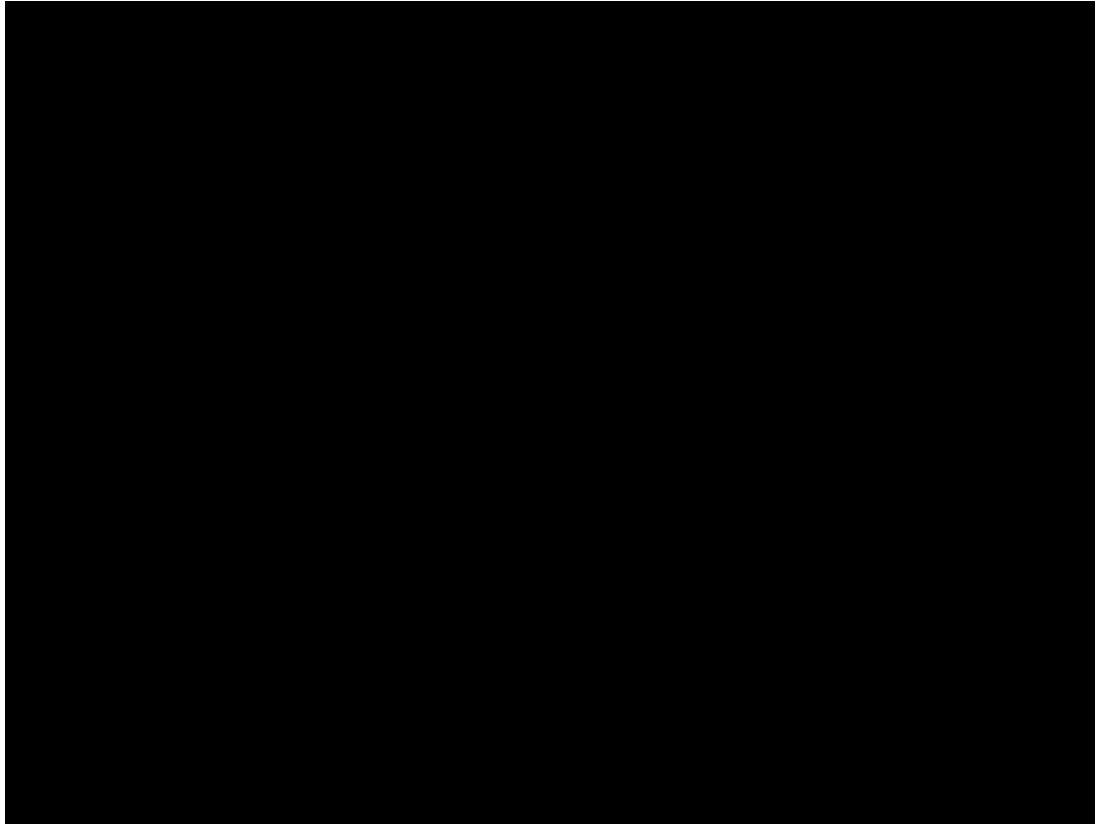


# RRT\*

- RRT\* was used for Milestone 3 with following features:
  - Angle Constraints in steering function
  - Velocity calculated based on path length and speed
  - Early stopping - direct to goal
  - Path Freezing until collision detection or completion
  - Occ-grid dilation
- Pure pursuit used to set goals for RRT\* with some lookahead
- Issues with tracking, single-threaded approach

# Result:

---





# Milestone 4 approach

---

# Overall idea

---

- Trajectory Selection
  - Local Trajectories Generation
  - Local Path selection to track Global Path
- MPC controller
  - Reference Tracking controller
- Lane Switching

# Trajectory Selection

- Global Path
  - CMA-ES trajectory + Alternate parallel lanes
- Local Paths
  - Generated constant curvature paths offline
  - Drift minimal curves with fixed velocity



*Mini-HRHC paths*

# Trajectory Selection

- Path selection
  - Selected the local reference path which maximizes the objective
- Objective:
  - Closeness to the global path + maximizing progress + incremental index
  - (prevents moving far from global) (promotes going far along global) (prevents reversal)

# MPC Controller

## ➤ Cost function

- Quadratic Cost

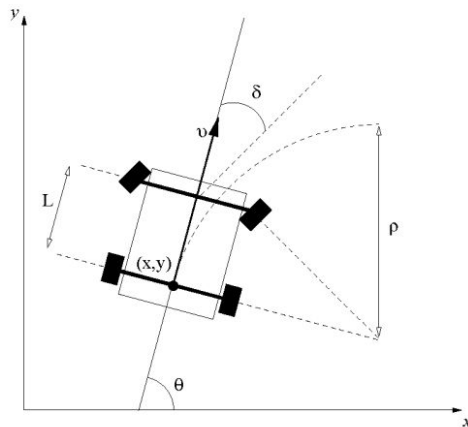
$$\sum_{k=0}^{N-1} (\mathbf{x}_k - \mathbf{x}_{ref,k})^T \mathbf{Q} (\mathbf{x}_k - \mathbf{x}_{ref,k}) + (\mathbf{u}_k - \mathbf{u}_{ref,k})^T \mathbf{R} (\mathbf{u}_k - \mathbf{u}_{ref,k})$$

- Large state costs (x,y; orientation not penalized)
- Small input costs (higher for orientation, near zero for v)
  - Desired input held at a constant high speed

# MPC Constraints

## ➤ Dynamics of System

- Kinematic Model with  $x, y, \Theta$
- Linearized using Forward Euler Discretization (proved to be accurate if  $t \approx 200\text{ms}$ )



$$\dot{x} = v \cos(\psi)$$

$$\dot{y} = v \sin(\psi)$$

$$\dot{\psi} = v \tan(\delta) / C_L$$

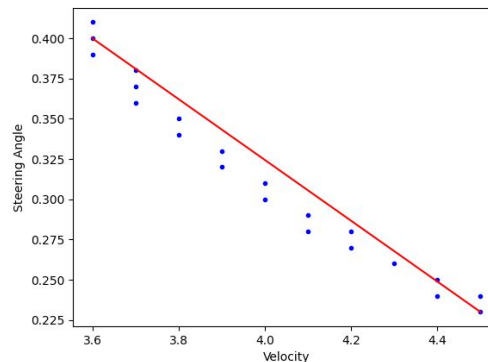
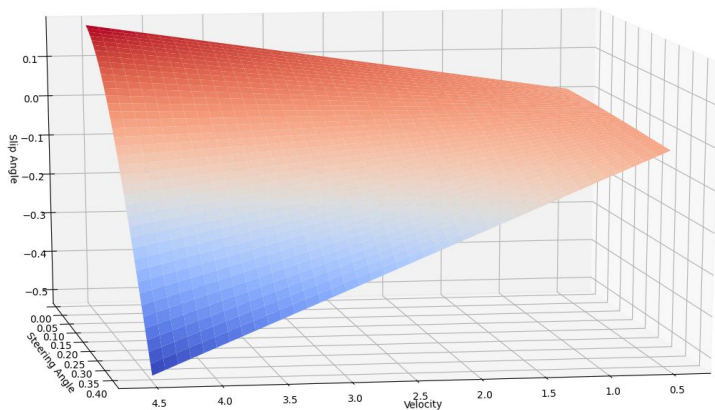
$$x = [x, y, \psi]^T$$

$$u = [v, \delta]^T$$



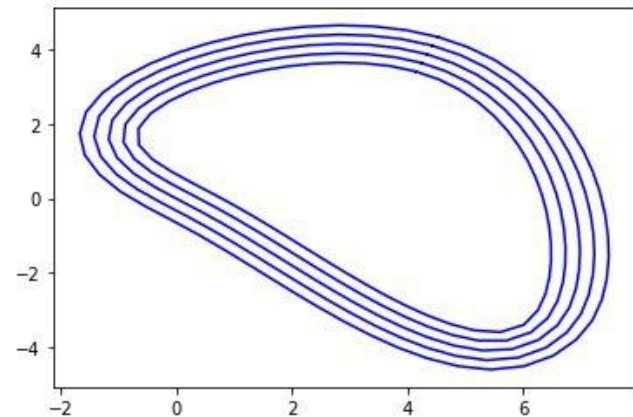
# MPC Constraints

- Steering vs Velocity Constraints
  - Non-linear, but kind of close
  - Set to infinity in final race parameters



# Lane Changing backup

- Why?
  - Current CMA-ES trajectory might be blocked by opponent
- Our solution
  - Keep 5 backup concentric paths which serve as lanes and switch tracking them on the fly
  - Use lookahead for collision on current path



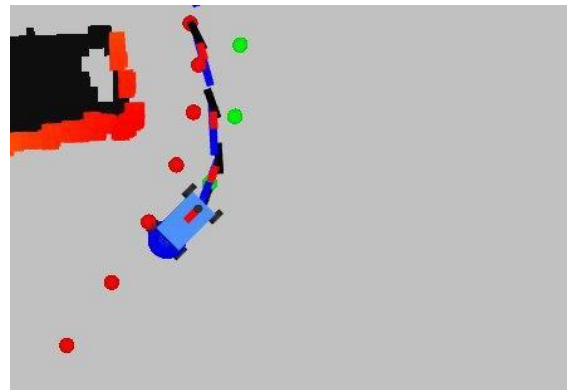
# Other features

## ➤ Multithreading

- Have a detached thread publishing on /drive in an infinite loop at 50Hz
- Use remainder of previous MPC solution outputs before current MPC finishes solving
  - Anytime Algorithm!

## ➤ Visualizations

- Car positions as calculated by QP solution
- Lane changes



# Results





# Miscellaneous

---

# Testing Methodology

---

- First test in I-P simulator when running in debugger
  - Find edge cases and fix them
  - Use pose estimate and place vehicle in different positions
  - Add obstacles to course
- Run in 2-P Gym simulator
  - Use gdb attach if problems show up
- Race against our old agents
  - Issues with passing slower agents or unpredictable ones

# Cutting Room Floor - Unused Material

## ➤ Prediction

- Using Gaussian Process model trained over a bundle of trajectories generated using CMA-ES
- Predicts  $dx/dt$  and  $dy/dt$  in real time for half the loop
- Shortcoming: needs several priors about opponent trajectory, model size  $> 1.5\text{GB}$ , difficult to incorporate with planner

## ➤ Half space constraints for MPC

- Couldn't figure out a suitable formulation to use for collision prevention

# Cutting Room Floor - Unused Material

- RRT\* as MPC Backup
  - Used regularized cubic splines to interpolate between trajectory points for smoothing
  - Applied randomized shortcutting algorithm to reduce path length safely
  - Issues: Couldn't get MPC to track the trajectory reliably

## Fast Smoothing of Manipulator Trajectories using Optimal Bounded-Acceleration Shortcuts

Kris Hauser\* and Victor Ng-Thow-Hing†

\* School of Informatics and Computing, Indiana University, Bloomington, IN 47405 USA

† Honda Research Institute, Mountain View, CA 94041 USA

**Abstract**—This paper considers a shortcutting heuristic to smooth jerky trajectories for many-DOF robot manipulators subject to collision constraints, velocity bounds, and acceleration bounds. The heuristic repeatedly picks two points on the trajectory and attempts to replace the intermediate trajectory with a shorter, collision-free segment. Here, we construct segments that interpolate between endpoints with specified velocity in a time-optimal fashion, while respecting velocity and acceleration bounds. These trajectory segments consist of parabolic and straight-line curves, and can be computed in closed form. Experiments on reaching tasks in cluttered human environments demonstrate that the technique can generate smooth, collision-free, and natural-looking motion in seconds for a PUMA manipulator and the Honda ASIMO robot.

### I. INTRODUCTION

Autonomous robots that interact with humans or human environments must have the capability to quickly generate safe and natural-looking motion. So far, it has been a challenge to simultaneously satisfy the three objectives of speed, safety, and esthetics for high-DOF robots performing complex tasks in unstructured environments. Sample-based planners (e.g., PRM, RRT, etc., see Chapter 7 of [1]) are widely used to plan collision-free paths for high-DOF robots. They are often fast, but they produce jerky, unnatural paths. This paper presents a fast smoothing algorithm that postprocesses paths to produce a dynamic trajectory that respects velocity and acceleration bounds and avoids collision.

Standard sample-based planners compute piecewise linear paths that can be executed physically by controlling the robot at

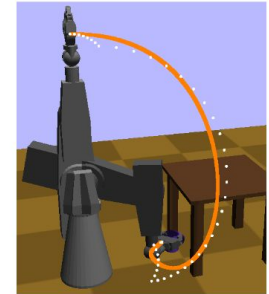
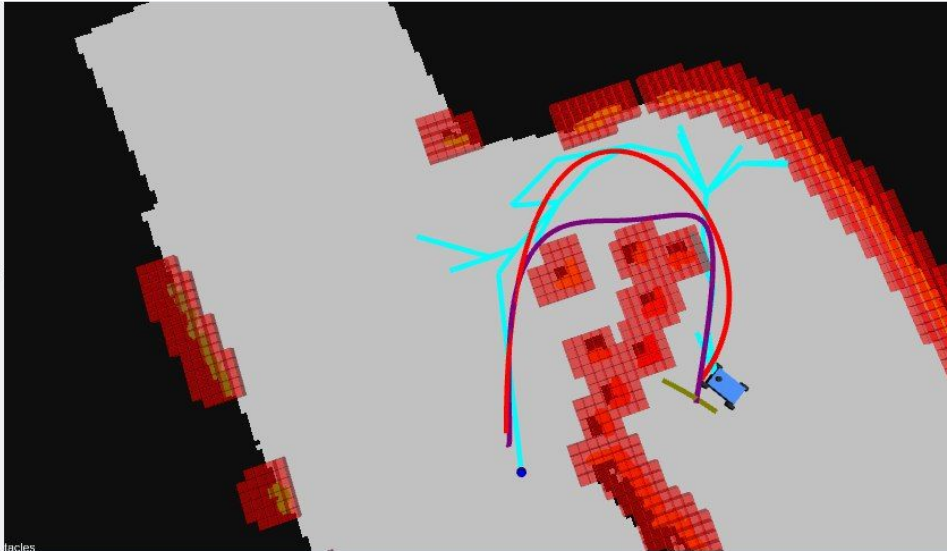


Fig. 1. A manipulator reaches under a table to grasp a cup. The white dotted curve depicts the original end effector path. The orange curve depicts the smoothed path after 100 randomly-attempted shortcuts. Execution time is reduced from 9.4s to 4.0s.

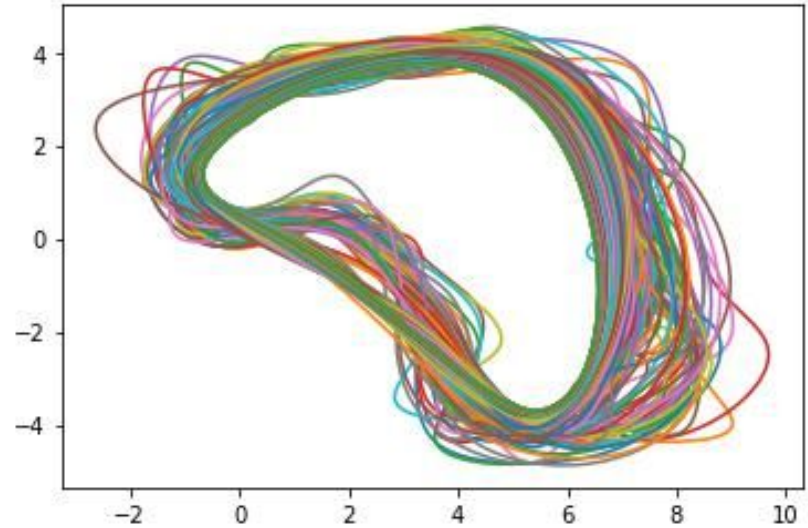
the algorithm is a smooth trajectory that respects collision, velocity, and acceleration constraints.



# Cutting Room Floor - Unused Material

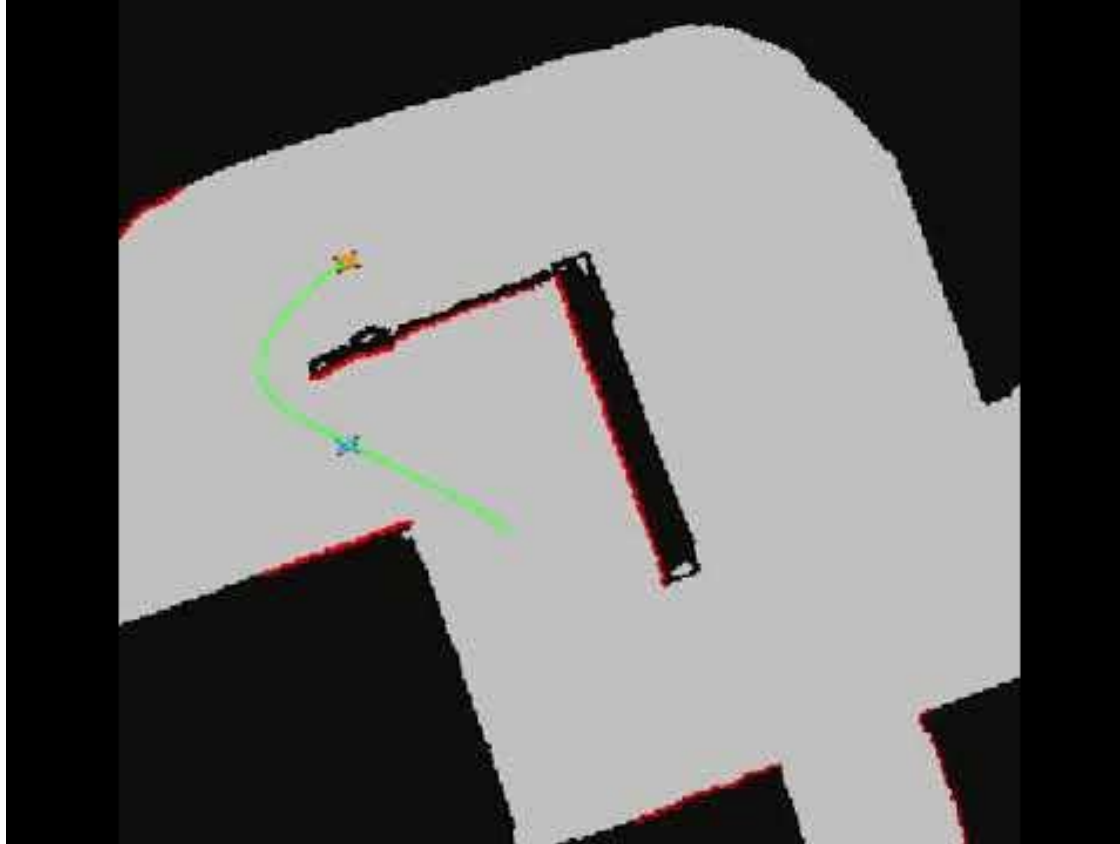


Red - Splined RRT\*, Purple - Shortcut & Splined RRT\*



Trajectories sampled for training a Gaussian Process

# Cutting Room Floor - Unused Material

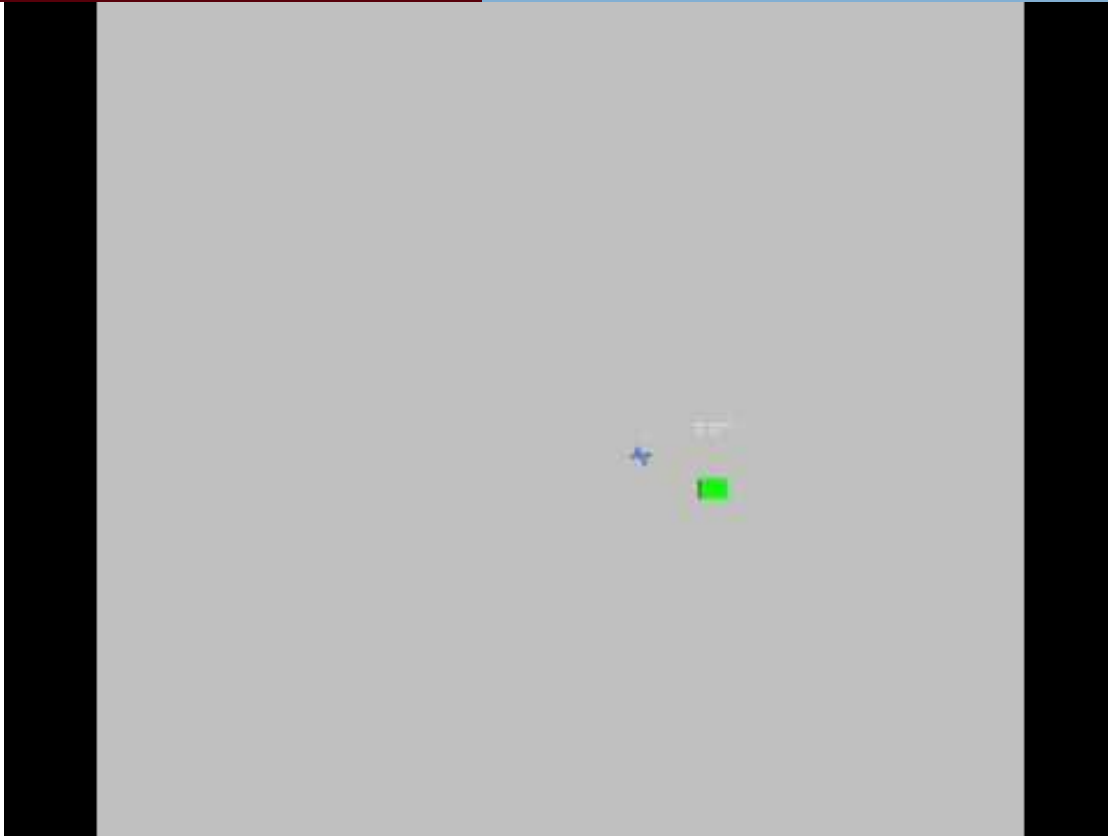


# Learning Experiences

---

- (Dynamically feasible) RRT\* is hard to get right
- Start simple before complicated solutions
- Use classes and objects liberally for C++ codebase
- Always use run with GDB when trying new things!
- Using visualizations helps a lot with debugging
- Learn to use the right tool for programming and collaborating
- Unit tests **would have** saved a LOT of time
- “Brilliance is knowing when to stop” - \_anon (2020)

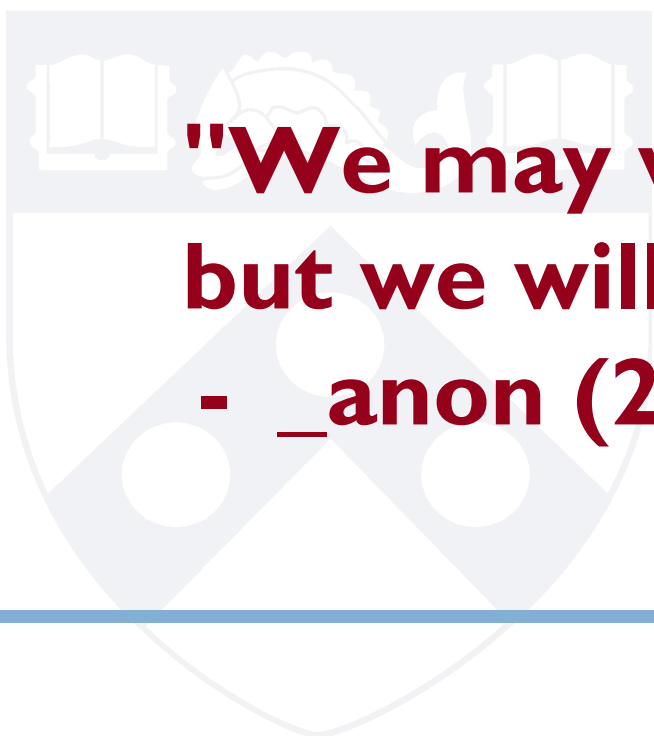
# Something Silly



# Acknowledgements

---

Thank you TAs for all your hard work for making this learning experience possible and Prof. Rahul for this opportunity.



**"We may win and we may lose,  
but we will never be defeated."  
- \_anon (2020)**

THANK YOU

---

---

“Questions, Comments, and Concerns?”

# References

1. MPC Lecture slides:  
[https://docs.google.com/presentation/d/1TcleCBkHEoWMcvqRlykKvhhI7tIENiC6Xy\\_UVFI3ppl/edit#slide=id.p30](https://docs.google.com/presentation/d/1TcleCBkHEoWMcvqRlykKvhhI7tIENiC6Xy_UVFI3ppl/edit#slide=id.p30)
2. Alexander Domahidi Alexander Liniger and Manfred Morari. Optimization-based autonomous racing of 1:43 Scale rc cars. November 2017
3. Thomas Lipp and Stephen Boyd. Minimum-time speed optimisation over a fixed path. International Journal of Control, 87(6):1297–1311, 2014
4. Achin Jain Joseph Auckley Kim Luong Matthew O’Kelly, Hongrui Zheng and Rahul Mangharam. Tech report: Tunercar: A superoptimization toolchain for autonomous racing. September 2019.
5. Goli, S. A., Far, B. H., & Fapojuwo, A. O. (2018). Vehicle Trajectory Prediction with Gaussian Process Regression in Connected Vehicle Environment. IEEE Intelligent Vehicles Symposium, Proceedings, 2018-June(Iv), 550–555. <https://doi.org/10.1109/IVS.2018.8500614>
6. Hauser, K., & Ng-Thow-Hing, V. (2010). Fast smoothing of manipulator trajectories using optimal bounded-acceleration shortcuts. Proceedings - IEEE International Conference on Robotics and Automation, 2493–2498. <https://doi.org/10.1109/ROBOT.2010.5509683>